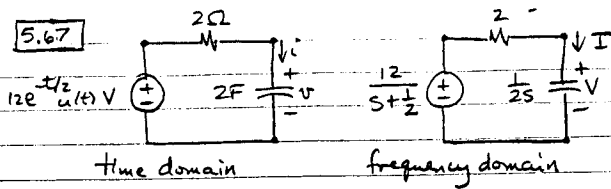


5.67



By voltage division,

$$V = \frac{\frac{1}{2s}}{2 + \frac{1}{2s}} \cdot \frac{12}{s + \frac{1}{2}} = \frac{1}{4s + 1} \cdot \frac{12}{s + \frac{1}{2}} = \frac{3}{(s + \frac{1}{4})(s + \frac{1}{2})}$$

$$V = \frac{3}{(s + \frac{1}{4})(s + \frac{1}{2})} = \frac{k_1}{s + \frac{1}{4}} + \frac{k_2}{s + \frac{1}{2}}$$

$$k_1 = \frac{3}{s + \frac{1}{2}} \Big|_{s = -\frac{1}{4}} = \frac{3}{-\frac{1}{2} + \frac{1}{2}} = 12 \quad k_2 = \frac{3}{s + \frac{1}{4}} \Big|_{s = -\frac{1}{2}} = \frac{3}{-\frac{1}{2} + \frac{1}{4}} = -12$$

$$\therefore V = \frac{12}{s + \frac{1}{4}} - \frac{12}{s + \frac{1}{2}} \Rightarrow v(t) = 12e^{-t/4} - 12e^{-t/2} u(t)$$

$$v(t) = (12e^{-t/4} - 12e^{-t/2}) u(t) \text{ V}$$

$$I = \frac{V}{1/2s} = 2sV = 2s \cdot \frac{3}{(s + \frac{1}{4})(s + \frac{1}{2})}$$

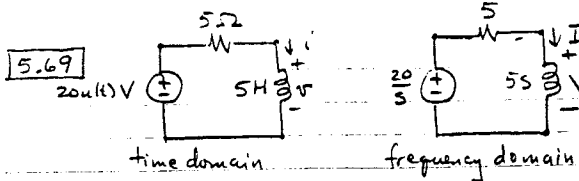
$$I = \frac{6s}{(s + \frac{1}{4})(s + \frac{1}{2})} = \frac{k_1}{s + \frac{1}{4}} + \frac{k_2}{s + \frac{1}{2}}$$

$$k_1 = \frac{6s}{s + \frac{1}{2}} \Big|_{s = -\frac{1}{4}} = \frac{6(-\frac{1}{4})}{-\frac{1}{4} + \frac{1}{2}} = -6 \quad k_2 = \frac{6s}{s + \frac{1}{4}} \Big|_{s = -\frac{1}{2}} = \frac{6(-\frac{1}{2})}{-\frac{1}{2} + \frac{1}{4}} = 12$$

$$\therefore I = \frac{-6}{s + \frac{1}{4}} + \frac{12}{s + \frac{1}{2}} \Rightarrow i(t) = -6e^{-t/4} + 12e^{-t/2} u(t)$$

$$i(t) = (-6e^{-t/4} + 12e^{-t/2}) u(t) \text{ A}$$

5.69



By KVL, $\frac{20}{s} = 5I + 5sI = (5s + 5)I$

$$\therefore I = \frac{20/s}{5s + 5} = \frac{4}{s(s + 1)} = \frac{k_1}{s} + \frac{k_2}{s + 1}$$

$$k_1 = \frac{4}{s + 1} \Big|_{s=0} = 4 \quad k_2 = \frac{4}{s} \Big|_{s=-1} = -4$$

$$I = \frac{4}{s} - \frac{4}{s + 1} \Rightarrow i(t) = 4u(t) - 4e^{-t} u(t)$$

$$i(t) = (4 - 4e^{-t}) u(t) \text{ A}$$

$$V = 5sI = 5s \left(\frac{4}{s(s + 1)} \right) = \frac{20}{s + 1} \Rightarrow v(t) = 20e^{-t} u(t) \text{ V}$$

5.110 $H(s) = \frac{s}{s + 2}$

(a) $x(t) = u(t) \Rightarrow X(s) = \frac{1}{s}$

$$\therefore Y(s) = H(s)X(s) = \frac{s}{s + 2} \cdot \frac{1}{s} = \frac{1}{s + 2} \Rightarrow y(t) = e^{-2t} u(t)$$

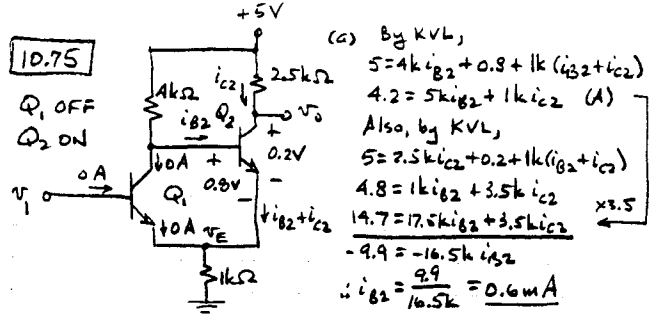
(b) $x(t) = e^{-t} u(t) \Rightarrow X(s) = \frac{1}{s + 1}$

$$\therefore Y(s) = H(s)X(s) = \frac{s}{s + 2} \cdot \frac{1}{s + 1} = \frac{s}{(s + 1)(s + 2)} = \frac{k_1}{s + 1} + \frac{k_2}{s + 2}$$

$$k_1 = \frac{s}{s + 2} \Big|_{s = -1} = \frac{-1}{-1 + 2} = -1 \quad k_2 = \frac{s}{s + 1} \Big|_{s = -2} = \frac{-2}{-2 + 1} = 2$$

$$Y(s) = \frac{-1}{s + 1} + \frac{2}{s + 2} \Rightarrow y(t) = -e^{-t} u(t) + 2e^{-2t} u(t) = (-e^{-t} + 2e^{-2t}) u(t)$$

10.75



(a) By KVL,
 $5 = 4k i_{B2} + 0.2 + 1k (i_{B2} + i_{C2})$
 $4.2 = 5k i_{B2} + 1k i_{C2} \quad (A)$
 Also, by KVL,
 $5 = 2.5k i_{C2} + 0.2 + 1k (i_{B2} + i_{C2})$
 $4.8 = 1k i_{B2} + 3.5k i_{C2}$
 $19.7 = 17.5k i_{B2} + 3.5k i_{C2}$
 $-9.9 = -16.5k i_{B2}$
 $\therefore i_{B2} = \frac{9.9}{16.5k} = 0.6 \text{ mA}$

From Equation (A), $1k i_{C2} = 4.2 - 5k i_{B2} = 4.2 - 5k(0.6 \text{ mA}) = 1.2$
 $\therefore i_{C2} = \frac{1.2}{1k} = 1.2 \text{ mA}$

For Q_2 to indeed be ON, $hFE_2 \geq \frac{i_{C2}}{i_{B2}} = \frac{1.2 \text{ mA}}{0.6 \text{ mA}} = 2$

(b) Q_2 ON $\Rightarrow v_0$ is low.

By KVL, $v_0 = 0.2 + 1k (i_{B2} + i_{C2}) = 0.2 + 1k(0.6 \text{ mA} + 1.2 \text{ mA}) = 0.2 + 1.8$
 $v_0 = 2 \text{ V}$ is the low voltage

(c) v_0 will remain low as long as Q_1 is OFF ($v_{BE1} < 0.5 \text{ V}$)

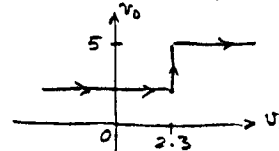
Thus, $v_{BE1} < 0.5$

$v_1 - v_E < 0.5$

$v_1 < 0.5 + v_E = 0.5 + 1k (i_{B2} + i_{C2}) = 0.5 + 1k(0.6 \text{ mA} + 1.2 \text{ mA})$

$v_1 < 0.5 + 1k(1.8 \text{ mA}) = 0.5 + 1.8 = 2.3 \text{ V}$ is the upper threshold voltage

When $v_1 > 2.3 \text{ V}$, then v_0 goes high (5V).

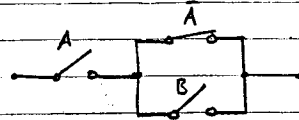


11.19

A	B	C	$L = AB + AC$
0	0	0	0
0	0	1	0
0	1	0	0
0	1	1	0
1	0	0	0
1	0	1	1
1	1	0	1
1	1	1	1

Since this is identical to Table 11.4, then $AB + AC = A(B + C)$

11.23



A	\bar{A}	B	$L = A(\bar{A} + B) \Rightarrow A(\bar{A} + B) = AB$
0	1	0	0
0	1	1	0
1	0	0	0
1	0	1	1

11.27 $F = (A + B)(\bar{A}B)$

A	B	AB	$\bar{A}B$	A + B	$F = (A + B)(\bar{A}B)$
0	0	0	1	0	0
0	1	0	1	1	1
1	0	0	1	1	1
1	1	1	0	1	0

This is the exclusive-OR operation.