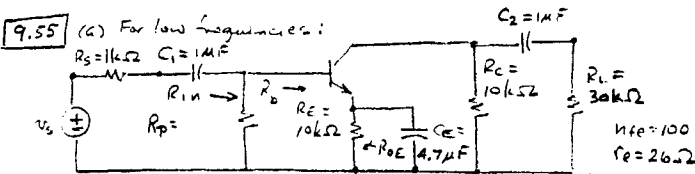


9.55 (a) For low frequencies:



ac-equivalent circuit  
 $R_p = 60k \parallel 30k = \frac{(60k)(30k)}{60k + 30k} = 20k\Omega$   
 $R_{in} = R_p \parallel R_b = \frac{(20k)(2.63k)}{20k + 2.63k} = 2.32k\Omega$   
 For input lead network,  $\omega_1 = \frac{1}{(R_{in} + R_1)C_1} = \frac{1}{(1k + 2.32k)\mu} = 301 \text{ rad/s}$

For output lead network,  $\omega_2 = \frac{1}{(R_c + R_L)C_2} = \frac{1}{(10k + 30k)\mu} = 25 \text{ rad/s}$   
 $R_{0E} = R_E \parallel (r_e + \frac{R}{1+h_{fe}}) = 10k \parallel (1.5\Omega + \frac{95\Omega}{101}) = 10k \parallel 35.4 = 353\Omega$

For bypass capacitor,  $\omega_3 = \frac{1}{R_{0E}C_E} = \frac{1}{(353)(4.7\mu)} = 6.03 \text{ krad/s}$

Thus,  $\omega_L = 6.03 \text{ krad/s}$  ( $f_L = 960 \text{ Hz}$ )

(b)  $A = g_m R_T = \frac{R_T}{r_e} = \frac{R_c \parallel R_L}{r_e} = \frac{10k \parallel 30k}{26} = \frac{7.5k}{26} = 288$   $C_c = 5 \text{ pF}$

$C_c + C_e = \frac{1}{2\pi f_c R_T} = \frac{1}{2\pi(30k)(110\Omega)} = 5 \text{ pF} \Rightarrow C_e = 5 \text{ pF} - 5 \text{ pF} = 0 \text{ pF}$

$r_{\pi} = (1+h_{fe})r_e = 101(26) = 2.63k\Omega$   
 $R_g = (R_c \parallel R_p) \parallel r_{\pi} = 952 \parallel 2.63k = \frac{(952)(2.63k)}{952 + 2.63k} = 699\Omega$

$C_g = C_e + (1+A)C_c = 46 \text{ pF} + 101(5 \text{ pF}) = 1491 \text{ pF}$

$\omega_g = \frac{1}{R_g C_g} = \frac{1}{(699)(1491 \text{ pF})} = 400 \text{ krad/s}$  for input lag network

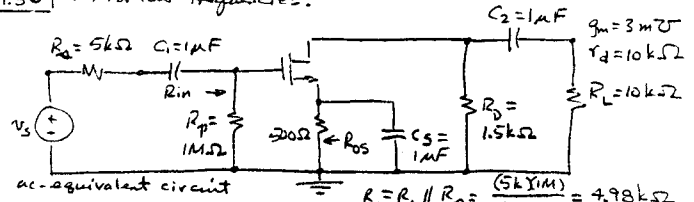
$C_T = \frac{1+A}{A} C_c = \frac{289}{288} 5 \text{ pF} = 5 \text{ pF}$   $r_T = 10k \parallel 30k = 7.5k\Omega$

$\omega_T = \frac{1}{r_T C_T} = \frac{1}{(7.5k)(5 \text{ pF})} = 26.7 \text{ Mrad/s}$  for output lag network

Thus,  $\omega_H = 960 \text{ krad/s}$  ( $f_H = 152 \text{ kHz}$ )

(c)  $BW = \omega_H - \omega_L = 960 \text{ krad/s} - 25 \text{ rad/s} \approx 960 \text{ krad/s}$  ( $152 \text{ kHz}$ )

9.56 (a) For low frequencies:



ac-equivalent circuit  
 $R_g = R_0 \parallel R_p = \frac{(5k)(1M)}{5k + 1M} = 4.98k\Omega$   
 $R_p = 2M \parallel 2M = 1M\Omega$   $R_{in} = R_p = 1M\Omega$   $r_d \parallel R_D = \frac{(10k)(1.5k)}{10k + 1.5k} = 1.3k\Omega$   
 For input lead network,  $\omega_1 = \frac{1}{(R_{in} + R_1)C_1} = \frac{1}{(1M + 5k)\mu} = 0.995 \text{ rad/s}$

For output lead network,  $\omega_2 = \frac{1}{(R_D \parallel R_L + R_L)C_2} = \frac{1}{(1.3k + 10k)\mu} = 88.5 \text{ rad/s}$

$R_{0S} = R_S \parallel \frac{1}{g_m} \parallel r_d = 500 \parallel \frac{1}{3m} \parallel 10k = 200 \parallel 333 \parallel 10k = 196\Omega$

For the bypass capacitor,  $\omega_3 = \frac{1}{R_{0S}C_S} = \frac{1}{(196)(1\mu)} = 5.1 \text{ krad/s}$

Thus,  $\omega_L = 5.1 \text{ krad/s}$  ( $f_L = 812 \text{ Hz}$ )

(b)  $R_T = r_d \parallel R_D \parallel R_L = 10k \parallel 1.5k \parallel 10k = 5k \parallel 1.5k = 1.15k\Omega$   
 $A = g_m R_T = (3m)(1.15k) = 3.45$   $R_g = R_0 \parallel R_p = 5k \parallel 1M = \frac{(5k)(1M)}{5k + 1M} = 4.95k\Omega$

$C_g = C_{ga} + (1+A)C_{gd} = 2 \text{ pF} + (1+3.45)3 \text{ pF} = 15.4 \text{ pF}$

$C_T = C_{da} + \frac{1+A}{A} C_{gd} = 1 \text{ pF} + \frac{4.45}{3.45} 3 \text{ pF} = 4.87 \text{ pF}$

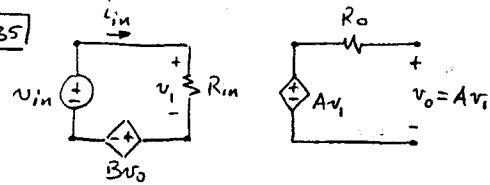
$\omega_g = \frac{1}{R_g C_g} = \frac{1}{(4.95k)(15.4 \text{ pF})} = 13 \text{ Mrad/s}$  for input lag network

$\omega_T = \frac{1}{r_T C_T} = \frac{1}{(1.15k)(4.87 \text{ pF})} = 178 \text{ Mrad/s}$  for output lag network

Thus,  $\omega_H = 13 \text{ Mrad/s}$  ( $2.07 \text{ MHz}$ )

(c)  $BW = \omega_H - \omega_L = 13M - 5.1k = 13 \text{ Mrad/s}$  ( $2.07 \text{ MHz}$ )

10.35



By KVL,  $V_{in} = V_1 + B V_0 \Rightarrow V_1 = V_{in} - B V_0 \Rightarrow V_0 = A(V_{in} - B V_0)$   
 $V_0 = A V_{in} - A B V_0$

$V_0 + A B V_0 = A V_{in}$   
 $V_0(1 + A B) = A V_{in}$

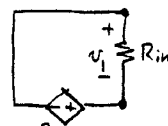
$\therefore \frac{V_0}{V_{in}} = \frac{A}{1 + A B} = A_F$

By KVL,

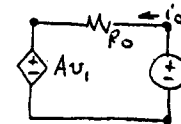
$V_{in} = R_{in} i_{in} + B V_0 = R_{in} i_{in} + B (\frac{A}{1 + A B} V_{in})$

$V_{in} - \frac{A B}{1 + A B} V_{in} = R_{in} i_{in}$

$\frac{1}{1 + A B} V_{in} = R_{in} i_{in} \Rightarrow \frac{V_{in}}{i_{in}} = (1 + A B) R_{in} = R_{if}$



$V_1 = -B V_0$



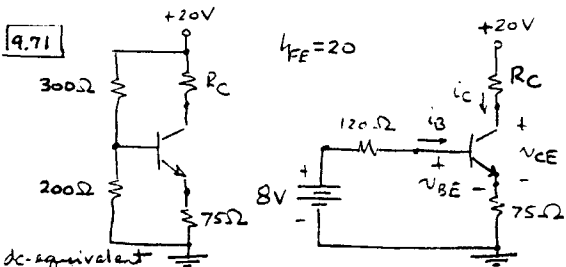
$V_0 = R_0 i_0 + A V_1 = R_0 i_0 + A(-B V_0)$

$V_0 + A B V_0 = R_0 i_0$

$V_0(1 + A B) = R_0 i_0$

$\frac{V_0}{i_0} = \frac{R_0}{1 + A B} = R_{of}$

9.71



dc-equivalent  
 (a)  $V_{CE} = \frac{200}{300+200}(20) = 9 \text{ V}$   $R_0 = 200\Omega \parallel 300\Omega = \frac{(200)(300)}{200+300} = 120\Omega$

By KVL,  
 $9 = 120 i_B + V_{BE} + 75(i_B + i_C)$

For active region,  $V_{BE} = 0.7 \text{ V}$ ,  $i_C = h_{FE} i_B = 20 i_B$

$9 = 120 i_B + 0.7 + 75(i_B + 20 i_B)$   
 $7.3 = 120 i_B + 1575 i_B = 1695 i_B \Rightarrow i_B = \frac{7.3}{1695} = 4.3 \text{ mA} = I_{BQ}$

$i_C = h_{FE} i_B = 20(4.3 \text{ mA}) = 86 \text{ mA} = I_{CQ}$

$V_{CE} = -R_C i_C + 20 - 75(i_B + i_C) = -R_C(86 \text{ mA}) + 20 - 75(21)(4.3 \text{ mA})$

$V_{CE} = -86 \text{ mA} R_C + 20 - 6.77 = -86 \text{ mA} R_C + 13.2 = V_{CEQ}$

$\frac{V_{CEQ}}{I_{CQ}} = R_T + R_E$   $R_T = R_C$   $R_E = 75\Omega$

$\frac{-86 \text{ mA} R_C + 13.2}{86 \text{ mA}} = R_C + 75$

$-R_C + \frac{13.2}{86 \text{ mA}} = R_C + 75$

$153 - 75 = 2 R_C \Rightarrow R_C = \frac{153 - 75}{2} = 39\Omega$

(b) From above,  $V_{CEQ} = 13.2 - 86 \text{ mA} R_C = 13.2 - 86 \text{ mA}(39) = 9.85 \text{ V}$

$P_0 = \frac{1}{2} V_{CEQ} I_{CQ} = \frac{1}{2}(9.85)(86 \text{ mA}) = 424 \text{ mW} = 0.424 \text{ W}$

(c)  $P_{D(max)} \geq V_{CEQ} I_{CQ} = (9.85)(86 \text{ mA}) = 847 \text{ mW} = 0.847 \text{ W}$

10.45  $A = 200,000$   $f_T = 1 \text{ MHz}$   $R_1 = 1 \text{ k}\Omega$

$$f_H = \frac{f_T}{A} = \frac{1 \text{ M}}{200,000} = \frac{1 \times 10^6}{2 \times 10^5} = 5 \text{ Hz}$$

$$B = \frac{R_1}{R_1 + R_2}$$

(a)  $R_2 = 9 \text{ k}\Omega$   $B = \frac{1 \text{ k}}{1 \text{ k} + 9 \text{ k}} = \frac{1}{10}$

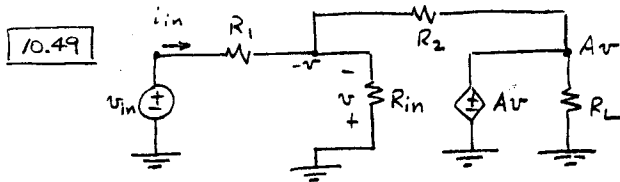
$$f_{HF} = (1 + AB)f_H = (1 + 200,000 \cdot \frac{1}{10}) 5$$

$$f_{HF} = (1 + 20,000) 5 = \underline{100 \text{ kHz}}$$

(b)  $R_2 = 1 \text{ M}\Omega$   $B = \frac{1 \text{ k}}{1 \text{ k} + 1 \text{ M}} = 9.99 \times 10^{-4}$

$$f_{HF} = (1 + AB)f_H = (1 + 200,000 [9.99 \times 10^{-4}]) 5$$

$$f_{HF} = \underline{1,000 \text{ Hz}}$$



By KCL at node  $-v$ ,

$$\frac{v_{in} + v}{R_1} + \frac{v}{R_{in}} + \frac{Av + v}{R_2} = 0$$

$$\frac{1}{R_1} v_{in} + \frac{v}{R_1} + \frac{v}{R_{in}} + \frac{Av + v}{R_2} = 0$$

$$\frac{1}{R_1} v_{in} = - \left( \frac{1}{R_1} + \frac{1}{R_{in}} + \frac{1+A}{R_2} \right) v$$

$$\therefore v = \frac{-\frac{1}{R_1} v_{in}}{\frac{1}{R_1} + \frac{1}{R_{in}} + \frac{1+A}{R_2}}$$

$$i_{in} = \frac{v_{in} + v}{R_1} \Rightarrow R_1 i_{in} = v_{in} + v = v_{in} - \frac{\frac{1}{R_1} v_{in}}{\frac{1}{R_1} + \frac{1}{R_{in}} + \frac{1+A}{R_2}}$$

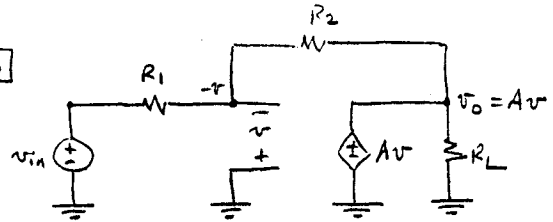
$$R_1 i_{in} = \left( \frac{1}{R_1} + \frac{1}{R_{in}} + \frac{1+A}{R_2} - \frac{1}{R_1} \right) v_{in}$$

$$\therefore \frac{v_{in}}{i_{in}} = \frac{R_1 \left( \frac{1}{R_1} + \frac{1}{R_{in}} + \frac{1+A}{R_2} \right)}{\frac{1}{R_1} + \frac{1}{R_{in}} + \frac{1+A}{R_2}} = \frac{1 + \frac{R_1}{R_{in}} + \frac{(1+A)R_1}{R_2}}{\frac{1}{R_1} + \frac{1+A}{R_2}}$$

$$R_{iF} = \frac{v_{in}}{i_{in}} = \frac{1 + \frac{R_1 R_2 + (1+A)R_1 R_{in}}{R_{in} R_2}}{\frac{R_2 + (1+A)R_{in}}{R_2}} = \frac{R_{in} R_2 + R_1 R_2 + (1+A)R_1 R_{in}}{R_2 + (1+A)R_{in}}$$

$$R_{iF} = \frac{R_{in} R_2}{R_2 + (1+A)R_{in}} + R_1 = R_1 + \frac{R_{in} \frac{R_2}{1+A}}{R_{in} + \frac{R_2}{1+A}} = \underline{R_1 + R_{in} \parallel \frac{R_2}{1+A}}$$

10.48



By KCL at node  $-v$ ,

$$-\frac{v - v_{in}}{R_1} + \frac{-v - Av}{R_2} = 0$$

$$R_2 v + R_2 v_{in} + R_1 v + A R_1 v = 0$$

$$R_2 v_{in} = (-R_1 - A R_1 - R_2) v$$

$$v = \frac{-R_2}{R_1 + A R_1 + R_2} v_{in}$$

$$\therefore v_o = Av = \frac{-A R_2}{R_1 + A R_1 + R_2} v_{in}$$

Hence,

$$A_F = \frac{v_o}{v_{in}} = \frac{-A R_2}{R_1 + A R_1 + R_2} = \underline{\underline{\frac{-R_2}{R_1 + \frac{R_1 + R_2}{A}}}}$$

10.54 (a)  $g_m = 5 \text{ mS}$ ,  $R = 100 \text{ k}\Omega$ ,  $f_0 = 1 \text{ kHz}$

$$g_m \geq \frac{29}{R_D} \Rightarrow R_D \geq \frac{29}{g_m} = \frac{29}{5 \text{ m}} = \underline{5.8 \text{ k}\Omega}$$

$$\omega_0 = \frac{1}{\sqrt{6} RC} \Rightarrow C = \frac{1}{\sqrt{6} \omega_0 R} = \frac{1}{\sqrt{6} (2\pi)(1 \text{ k})(100 \text{ k})} = \underline{650 \text{ pF}}$$

(b)  $g_m = 10 \text{ mS}$ ,  $C = 0.001 \mu\text{F}$ ,  $f_0 = 1 \text{ kHz}$

$$g_m \geq \frac{29}{R_D} \Rightarrow R_D \geq \frac{29}{g_m} = \frac{29}{10 \text{ m}} = \underline{2.9 \text{ k}\Omega}$$

$$\omega_0 = \frac{1}{\sqrt{6} RC} \Rightarrow R = \frac{1}{\sqrt{6} \omega_0 C} = \frac{1}{\sqrt{6} (2\pi)(1 \text{ k})(0.001 \mu)} = \underline{65 \text{ k}\Omega}$$

(c)  $R_D = 5 \text{ k}\Omega$ ,  $R = 100 \text{ k}\Omega$ ,  $C = 0.001 \mu\text{F}$

$$g_m \geq \frac{29}{R_D} = \frac{29}{5 \text{ k}} = \underline{5.8 \text{ mS}}$$

$$\omega_0 = \frac{1}{\sqrt{6} RC} = 2\pi f_0 \Rightarrow f_0 = \frac{1}{2\pi \sqrt{6} RC} = \frac{1}{2\pi \sqrt{6} (100 \text{ k})(0.001 \mu)}$$

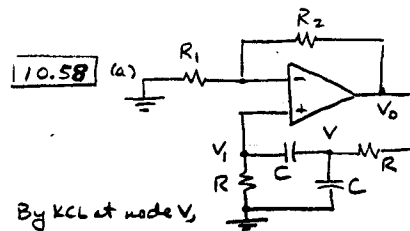
$$f_0 = \underline{650 \text{ Hz}}$$

(d)  $R_D = 5 \text{ k}\Omega$ ,  $R = 100 \text{ k}\Omega$ ,  $f_0 = 2 \text{ kHz}$

$$g_m \geq \frac{29}{R_D} = \frac{29}{5 \text{ k}} = \underline{5.8 \text{ mS}}$$

$$\omega_0 = \frac{1}{\sqrt{6} RC} \Rightarrow C = \frac{1}{\sqrt{6} \omega_0 R} = \frac{1}{\sqrt{6} (2\pi)(2 \text{ k})(100 \text{ k})}$$

$$C = \underline{325 \text{ pF}}$$



By KCL at node  $V_1$ ,

$$\frac{V_1}{R} + \frac{V_1 - V}{j\omega C} = 0$$

$$V_1 + j\omega RC V_1 - j\omega RC V = 0$$

$$(1 + j\omega RC)V_1 = j\omega RC V$$

$$V = \frac{1 + j\omega RC}{j\omega RC} V_1$$

By KCL at node  $V$ ,

$$\frac{V - V_1}{j\omega C} + \frac{V}{j\omega C} + \frac{V - V_0}{R} = 0$$

$$j\omega RC V - j\omega RC V_1 + j\omega RC V + V - V_0 = 0$$

$$(1 + j\omega 2RC)V - j\omega RC V_1 = V_0$$

$$(1 + j\omega 2RC) \frac{(1 + j\omega RC)}{j\omega RC} V_1 - j\omega RC V_1 = V_0$$

$$[(1 + j\omega 2RC)(1 + j\omega RC) - (j\omega RC)^2] V_1 = j\omega RC V_0$$

$$[1 + j\omega 2RC + j\omega RC + 2(j\omega RC)^2 - (j\omega RC)^2] V_1 = j\omega RC V_0$$

$$\frac{V_1}{V_0} = \frac{j\omega RC}{1 + j\omega 3RC + (j\omega RC)^2} = \frac{1}{\frac{1}{j\omega RC} + 3 + j\omega RC}$$

$$\frac{V_1}{V_0} = \frac{1}{3 + j(\omega RC - \frac{1}{\omega RC})} = B$$

(b) Oscillation occurs when  $\omega RC = \frac{1}{\omega RC} \Rightarrow \omega^2 = \frac{1}{(RC)^2} \Rightarrow \omega_0 = \frac{1}{RC}$

(c) By KCL at the inverting input of the op amp,

$$\frac{V_1}{R_1} + \frac{V_1 - V_0}{R_2} = 0 \Rightarrow R_2 V_1 + R_1 V_1 - R_1 V_0 = 0$$

$$(R_1 + R_2) V_1 = R_1 V_0 \Rightarrow \frac{V_0}{V_1} = \frac{R_1 + R_2}{R_1} = 1 + \frac{R_2}{R_1} = A$$

When  $\omega = \frac{1}{RC}$ , then  $B = \frac{V_1}{V_0} = \frac{1}{3}$

For oscillation,  $AB = 1$  (minimum)

$$\left(1 + \frac{R_2}{R_1}\right) \frac{1}{3} = 1 \Rightarrow 1 + \frac{R_2}{R_1} = 3 \Rightarrow \frac{R_2}{R_1} = 2$$

$$\therefore \underline{\underline{R_2 = 2R_1}}$$