

2. $m\lambda = d \sin \theta \rightarrow m\lambda = d \sin 35^\circ = 0.574 d$. $\lambda/d = 0.574/m$. "Only" $\Rightarrow m=1$. So $\lambda/d = \mathbf{0.574}$

3. $\lambda = h/p = h/mc = 6.63 \times 10^{-28} \text{kg}\cdot\text{m/s} / (9.11 \times 10^{-31} \text{kg})(3 \times 10^8 \text{m/s}) = \mathbf{2.43 \times 10^{-12} \text{m}}$.

4. $qV = \frac{1}{2} m u^2 = \frac{(m u)^2}{2m} = \frac{p^2}{2m} = \frac{(h/\lambda)^2}{2m}$. Solve: $\lambda = \frac{h}{\sqrt{2mqV}}$

5. $p = h/\lambda = \frac{6.63 \times 10^{-34} \text{J}\cdot\text{s}}{10^{-6} \text{m}} = 6.63 \times 10^{-28} \text{kg}\cdot\text{m/s}$. $u = \frac{p}{m} = \frac{6.63 \times 10^{-28} \text{kg}\cdot\text{m/s}}{9.11 \times 10^{-31} \text{kg}} = \mathbf{728 \text{m/s}}$.

This is actually quite slow as free-electron speeds go.

8. $\text{KE} = \frac{p^2}{2m} \rightarrow 1.6 \times 10^{-13} \text{J} = \frac{p^2}{2(1.67 \times 10^{-27} \text{kg})} \Rightarrow p = 2.31 \times 10^{-20} \text{kg}\cdot\text{m/s}$.

$\frac{6.63 \times 10^{-34} \text{J}\cdot\text{s}}{2.31 \times 10^{-20} \text{kg}\cdot\text{m/s}} = \mathbf{2.87 \times 10^{-14} \text{m}}$. $20 \times 1.6 \times 10^{-19} \text{J} = \frac{p^2}{2(1.67 \times 10^{-27} \text{kg})}$

$\Rightarrow p = 1.03 \times 10^{-22} \text{kg}\cdot\text{m/s}$. $\frac{6.63 \times 10^{-34} \text{J}\cdot\text{s}}{1.03 \times 10^{-22} \text{kg}\cdot\text{m/s}} = \mathbf{6.41 \times 10^{-12} \text{m}}$.

10. $p = h/\lambda = \frac{6.63 \times 10^{-34} \text{J}\cdot\text{s}}{10^{-9} \text{m}} = 6.63 \times 10^{-25} \text{kg}\cdot\text{m/s}$. $u = \frac{p}{m} = \frac{6.63 \times 10^{-25} \text{kg}\cdot\text{m/s}}{9.11 \times 10^{-31} \text{kg}} = \mathbf{7.28 \times 10^5 \text{m/s}}$.

(b) Using result of exercise 4, $\lambda = \frac{h}{\sqrt{2mqV}} \rightarrow 10^{-9} \text{m} = \frac{6.63 \times 10^{-34} \text{J}\cdot\text{s}}{\sqrt{2(9.11 \times 10^{-31} \text{kg})(1.6 \times 10^{-19} \text{C})V}}$

$\Rightarrow V = \mathbf{1.5 \text{V}}$. In practice it is much higher than this, giving a smaller λ and better resolution.

11. $m\lambda = d \sin \theta$. Using result of exercise 4, $\lambda = \frac{h}{\sqrt{2mqV}} = \frac{6.63 \times 10^{-34} \text{J}\cdot\text{s}}{\sqrt{2(9.11 \times 10^{-31} \text{kg})(1.6 \times 10^{-19} \text{C})(54 \text{V})}} = 1.67 \times 10^{-10} \text{m}$. $1(1.67 \times 10^{-10} \text{m}) = d \sin 50^\circ \Rightarrow d = \mathbf{2.2 \times 10^{-10} \text{m}}$.

12. To find moon's speed, use $F=ma$. The gravitational force gives it centripetal acceleration:

$$G \frac{m_{\text{earth}} m_{\text{moon}}}{r^2} = m_{\text{moon}} \frac{v^2}{r} \Rightarrow v = \sqrt{\frac{G m_{\text{earth}}}{r}} = \sqrt{\frac{(6.67 \times 10^{-11} \text{N}\cdot\text{m}^2/\text{kg}^2)(5.98 \times 10^{24} \text{kg})}{3.84 \times 10^8 \text{m}}} =$$

$1.02 \times 10^3 \text{m/s}$. Thus $\lambda = h/p = \frac{6.63 \times 10^{-34} \text{J}\cdot\text{s}}{(7.35 \times 10^{22} \text{kg})(1.02 \times 10^3 \text{m/s})} = 8.85 \times 10^{-60} \text{m}$.

This is much smaller than the dimensions of the region in which it moves. In fact, as in the airplane's case in example 3.1, it is smaller than the atomic nucleus! The moon certainly **orbits as a classical particle**.

23. $\Delta x \Delta p \geq \frac{1}{2} \hbar \rightarrow (10^{-6} \text{m})(0.145 \text{kg}) \Delta v \geq \frac{1}{2} (1.055 \times 10^{-34} \text{J}\cdot\text{s}) \Rightarrow \Delta v \geq \mathbf{3.6 \times 10^{-28} \text{m/s}}$. $\frac{1 \text{nm}}{\text{billion centuries}}$

25. $\Delta x \Delta p \geq \frac{1}{2} \hbar \rightarrow (5 \times 10^{-15} \text{m})(1.67 \times 10^{-27} \text{kg}) \Delta v \geq \frac{1}{2} (1.055 \times 10^{-34} \text{J}\cdot\text{s}) \Rightarrow \Delta v \geq \mathbf{6.3 \times 10^6 \text{m/s}}$.

Its KE would be $\frac{1}{2} (1.67 \times 10^{-27} \text{kg})(6.3 \times 10^6 \text{m/s})^2 \approx 0.2 \text{MeV}$, on the low side of typical energies in the nucleus.

28. $\Delta x \Delta(mv) \geq \frac{1}{2} \hbar \rightarrow \Delta v \geq \frac{\hbar}{2m\Delta x} = \frac{\hbar}{2mL}$. The $\text{KE} \sim \frac{1}{2} m (\Delta v)^2 \geq \frac{\hbar^2}{8mL^2}$

30. $\theta_{\text{wave}} \cong \sin \theta_1 = \frac{1\lambda}{a} = \frac{h/(mv)}{a} = \frac{h}{mva}$. $\theta_{\text{part.}} = \frac{\Delta p_y}{p} \cong \frac{\frac{1}{2} \hbar / \Delta y}{p} = \frac{\frac{1}{2} \hbar / a}{mv} = \frac{h}{4\pi mva}$. $\frac{\theta_{\text{wave}}}{\theta_{\text{part.}}} = 4\pi$

49. $(\gamma_u - 1)mc^2 = mc^2 \Rightarrow \gamma_u = 2 \Rightarrow u = (\sqrt{3}/2) c$. $p = \gamma_u m u = 2(1.67 \times 10^{-27} \text{kg})(\sqrt{3}/2) c$

$= 8.68 \times 10^{-19} \text{kg}\cdot\text{m/s}$. $\lambda = h/p = \frac{6.63 \times 10^{-34} \text{J}\cdot\text{s}}{8.68 \times 10^{-19} \text{kg}\cdot\text{m/s}} = \mathbf{7.64 \times 10^{-16} \text{m}}$. This is smaller than the

proton's accepted approximate radius. Such a fast proton would certainly behave as a **particle**.