

18-1. See the sketch below. Using Eq. (18-1),

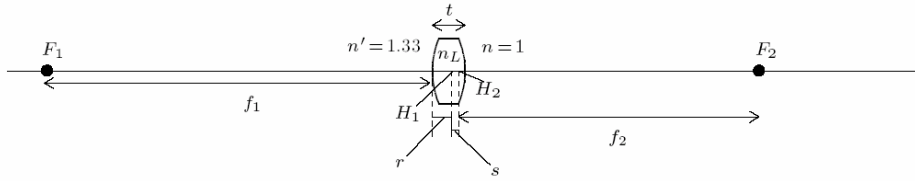
$$\frac{1}{f_1} = \frac{1.6 - 1}{1.33(-40 \text{ cm})} - \frac{1.6 - 1.33}{(1.33)(40 \text{ cm})} - \frac{(1.6 - 1.33)(1.6 - 1)}{1.33(1.6)} \frac{5 \text{ cm}}{(40 \text{ cm})(-40 \text{ cm})} \Rightarrow f_1 = -62.05 \text{ cm}$$

$$f_2 = -\frac{n'}{n} f_1 = -\frac{1}{1.33} (-62.05 \text{ cm}) = 46.66 \text{ cm}$$

Further, using Eq. (18-3),

$$r = \frac{n_L - n'}{n_L R_2} f_1 t = \frac{1.6 - 1}{1.6(-40 \text{ cm})} (-62.05 \text{ cm})(5 \text{ cm}) = 2.91 \text{ cm}$$

$$s = -\frac{n_L - n}{n_L R_1} f_2 t = \frac{1.6 - 1.33}{1.6(+40 \text{ cm})} (46.66 \text{ cm})(5 \text{ cm}) = -0.98 \text{ cm}$$



18-3. Using Eq. (18-1)

$$\frac{1}{f_1} = \frac{1.5 - 1}{10 \text{ cm}} - \frac{1.5 - 1}{-20 \text{ cm}} - \frac{(1.5 - 1)^2}{1.5} \frac{5 \text{ cm}}{(10 \text{ cm})(-20 \text{ cm})} \Rightarrow f_1 = 12.63 \text{ cm}$$

$$f_2 = -\frac{n'}{n} f_1 = -1(12.63 \text{ cm}) = -12.63 \text{ cm}$$

Further, using Eq. (18-3),

$$r = \frac{n_L - n'}{n_L R_2} f_1 t = \frac{1.5 - 1}{1.5(10 \text{ cm})} (12.63 \text{ cm})(5 \text{ cm}) = 2.105 \text{ cm}$$

$$s = -\frac{n_L - n}{n_L R_1} f_2 t = \frac{1.5 - 1}{1.5(-20 \text{ cm})} (-12.63 \text{ cm})(5 \text{ cm}) = -1.0525 \text{ cm}$$

Then $s_0 = 8 \text{ cm} + r = 10.105 \text{ cm}$ and,

$$-\frac{f_1}{s_0} + \frac{f_2}{s_i} = 1 \Rightarrow -\frac{12.63}{10.105} + \frac{(-12.63 \text{ cm})}{s_i} = 1 \Rightarrow s_i = -5.614 \text{ cm left of } H_2$$

That is $s_i = -5.614 \text{ cm} + s = -6.67 \text{ cm}$ left of V_2 . The magnification is,

$$m = -\frac{n s_i}{n' s_o} = -\frac{(1)(-5.614)}{(1)(10.105)} = +0.556$$

So, $h_i = m h_o = 0.556 \times 1 \text{ in} = 0.556 \text{ in}$.

18-9. The lens matrix is,

$$\begin{bmatrix} 1 & 0 \\ 1/10 & 1 \end{bmatrix} \begin{bmatrix} 1 & 5 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 \\ -1/10 & 1 \end{bmatrix} = \begin{bmatrix} 1/2 & 5/4 \\ -1/20 & 3/2 \end{bmatrix}$$

$$f_1 = 1/C = -20 \text{ cm}, \quad f_2 = -1/C = 20 \text{ cm}$$

$$q = -A/C = 10 \text{ cm}, \quad p = D/C = -30 \text{ cm}$$

$$r = (D - 1)/C = -10 \text{ cm}, \quad s = (1 - A)/C = -10 \text{ cm}$$

18-12. (a) The lens matrix is,

$$\begin{bmatrix} 1 & 15 \\ 0.5/(-4) & 3/2 \end{bmatrix} \begin{bmatrix} 1 & 8 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 30 \\ (-0.5)/(4 \times 1.5) & 2/3 \end{bmatrix} = \begin{bmatrix} 1/3 & 16/3 \\ -1/6 & 1/3 \end{bmatrix}$$

$$\begin{aligned} f_1 &= 1/C = -6 \text{ in}, \quad f_2 = -1/C = 6 \text{ in} \\ q &= -A/C = 2 \text{ in}, \quad p = D/C = -2 \text{ in} \\ r &= (D-1)/C = 4 \text{ in}, \quad s = (1-A)/C = -4 \text{ in} \end{aligned}$$

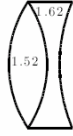
(b) Parallel light focuses at F_2 , measured from the output plane (or right surface) by $q = 2$ in.

18-14. (a), (b) The lens matrix is

$$\begin{bmatrix} 1 & 0 \\ 0.62/20 & 1.62 \end{bmatrix} \begin{bmatrix} 1 & 1/2 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 \\ -0.1/20 & 1.52 \end{bmatrix} \begin{bmatrix} 1 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 \\ -0.52/(20)(1.52) & 1/1.52 \end{bmatrix} = \begin{bmatrix} 0.9764 & 0.96755 \\ 0.009182 & 1.0333 \end{bmatrix}$$

$$\begin{aligned} f_1 &= 1/C = -150 \text{ cm}, \quad f_2 = -1/C = 150 \text{ cm} \\ q &= -A/C = 160 \text{ cm}, \quad p = D/C = -140 \text{ cm} \\ r &= (D-1)/C = 10 \text{ cm}, \quad s = (1-A)/C = 10 \text{ cm} \end{aligned}$$

(c) Consider each lens separately in air:



$$\begin{aligned} \frac{1}{f} &= \frac{n_2 - n_1}{n_1} \left(\frac{1}{R_1} - \frac{1}{R_2} \right) \Rightarrow \frac{1}{f_1} = \frac{1.52 - 1}{1} \left(\frac{1}{20 \text{ cm}} - \frac{1}{-20 \text{ cm}} \right) = 0.052 \text{ cm}^{-1} \\ \frac{1}{f_2} &= \frac{1.62 - 1}{1} \left(\frac{1}{-20 \text{ cm}} - \frac{1}{20 \text{ cm}} \right) = -0.062 \text{ cm}^{-1} \\ \text{Equivalent focal length: } \frac{1}{f_{\text{eq}}} &= \frac{1}{f_1} + \frac{1}{f_2} = 0.052 \text{ cm}^{-1} - 0.062 \text{ cm}^{-1} \Rightarrow f_{\text{eq}} = -100 \text{ cm} \end{aligned}$$

4-11. Generally, $\mathbf{k} \cdot \mathbf{r} = k_x x + k_y y + k_z z$.

(a) For propagation along the z -axis, $k_x = k_y = 0$. So $\mathbf{k} \cdot \mathbf{r} = k_z z$, with $k_z = 2\pi/\lambda$. The waveform can then be written as,

$$\psi = A \sin(\mathbf{k} \cdot \mathbf{r} - \omega t) = A \sin(k_z z - \omega t) = A \sin \left[\frac{2\pi}{\lambda}(z - vt) \right] = A \sin 2\pi(z/\lambda - vt)$$

(b) In this case, $k_z = 0$ and $k_x = k_y = |k|/\sqrt{2} = \frac{1}{\sqrt{2}} \frac{2\pi}{\lambda}$. The general form of the wave is then,

$$\psi = A \sin(\mathbf{k} \cdot \mathbf{r} \pm \omega t) = A \sin(k_x x + k_y y \pm \omega t) = A \sin \left[\frac{2\pi}{\sqrt{2}\lambda}(x + y \pm vt) \right] = A \sin 2\pi \left(\frac{x}{\sqrt{2}\lambda} + \frac{y}{\sqrt{2}\lambda} \pm vt \right).$$

If one is interested in the wave displacement only on the line $x = y$,

$$\psi = A \sin 2\pi \left(\frac{2x}{\sqrt{2}\lambda} \pm vt \right).$$

(c) In this case $\mathbf{k} = \frac{k}{\sqrt{3}}(\hat{x} + \hat{y} + \hat{z})$ and $\mathbf{k} \cdot \mathbf{r} = \frac{k}{\sqrt{3}}(x + y + z)$, with $k = 2\pi/\lambda$. The waveform is then,

$$\psi = A \sin(\mathbf{k} \cdot \mathbf{r} \pm \omega t) = A \sin \left[\frac{k}{\sqrt{3}}(x + y + z) \pm \omega t \right] = A \sin \left[\frac{2\pi}{\sqrt{3}\lambda}(x + y + z \pm vt) \right]$$

4-12. Let $\tilde{z} = a + ib$ where a and b are real.

(a) $(\tilde{z} + \tilde{z}^*)/2 = (a + ib + a - ib)/2 = a = \text{Re}(\tilde{z})$

(b) $(\tilde{z} - \tilde{z}^*)/2i = (a + ib - a + ib)/2i = b = \text{Im}(\tilde{z})$

(c) Let $\tilde{z} = e^{i\theta} = \cos \theta + i \sin \theta$ and apply the result from (a): $\cos \theta = (e^{i\theta} + e^{-i\theta})/2$

(d) Let $\tilde{z} = e^{i\theta} = \cos \theta + i \sin \theta$ and apply the result from (b): $\sin \theta = (e^{i\theta} - e^{-i\theta})/2i$

4-13. (a) Note that $e^{i\pi/2} = \cos(\pi/2) + i \sin(\pi/2) = i$ so that

$$i A e^{i(\mathbf{k} \cdot \mathbf{r} - \omega t + \varphi_0)} = e^{i\pi/2} A e^{i(\mathbf{k} \cdot \mathbf{r} - \omega t + \varphi_0)} = A e^{i(\mathbf{k} \cdot \mathbf{r} - \omega t + \varphi_0 + \pi/2)}$$

(b) Similarly, $e^{i\pi} = \cos(\pi) + i \sin(\pi) = -1$ so that

$$-A e^{i(\mathbf{k} \cdot \mathbf{r} - \omega t + \varphi_0)} = e^{i\pi} A e^{i(\mathbf{k} \cdot \mathbf{r} - \omega t + \varphi_0)} = A e^{i(\mathbf{k} \cdot \mathbf{r} - \omega t + \varphi_0 + \pi)}$$

5-4. One could proceed directly by mimicking the development for the cosine waves leading to Eqs. (5-9) and (5-10). I choose to first convert the given fields to the cosine form and then using those equations. That is,

$$y_1 = 5 \sin(\omega t + \pi/2) = 5 \cos(\omega t) = 5 \cos(0 - \omega t)$$

$$y_2 = 7 \sin(\omega t + \pi/3) = 7 \cos(\omega t + \pi/3 - \pi/2) = 7 \cos(\omega t - \pi/6) = 7 \cos(\pi/6 - \omega t)$$

Then using Eqs. (5-9) and (5-10):

$$y_0 = \sqrt{5^2 + 7^2 + 2 \cdot 5 \cdot 7 \cos(\pi/6)} = 11.6$$

$$\tan \alpha = \frac{0 + 7 \sin(\pi/6)}{5 + 7 \cos(\pi/6)} = \alpha = 0.098 \pi$$

$$y = 11.6 \cos(0.098 \pi - \omega t) = 11.6 \cos(\omega t - 0.098 \pi) = 11.6 \sin(\omega t - 0.098 \pi + \pi/2)$$

$$y = 11.6 \sin(\omega t + 0.402 \pi)$$

5-7. At the indicated position,

$$\psi_1 = A_1 \cos(8 \pi/3 - \omega t), \quad A_1 = 4 \text{ cm}, \omega = 20/\text{s}$$

$$\psi_2 = A_2 \cos(3 \pi/2 - \omega t), \quad A_2 = 2 \text{ cm}, \omega = 20/\text{s}$$

Using Eqs (5-9) and (5-10),

$$A = \sqrt{A_1^2 + A_2^2 + 2 A_1 A_2 \cos(\alpha_2 - \alpha_1)} = \sqrt{20 + 16 \cos(3 \pi/2 - 8 \pi/3)} \text{ cm} = 2.48 \text{ cm}$$

$$\tan \alpha = \frac{4 \sin(8 \pi/3) + 2 \sin(3 \pi/2)}{4 \cos(8 \pi/3) + 2 \sin(3 \pi/2)} \Rightarrow \alpha = 2.51$$

$$\psi_R = (2.48 \text{ cm}) \cos(2.51 - (20/\text{s}) t)$$