

- 11-15.** (a) According to Eq. (11-30) the condition for missing orders is, $a = (p/m)b$. The fourth order interference maxima are missing so $p = 4m$ and $a = 4b = 4(0.1 \text{ mm}) = 0.4 \text{ mm}$.
 (b) The irradiance is given by,

$$I = 4I_0 \left(\frac{\sin \beta}{\beta} \right)^2 \cos^2 \alpha$$

In zeroth order $I = 4I_0$. The interference maxima occur for,

$$p\lambda = a \sin \theta \Rightarrow \sin \theta = 0, \pm \lambda/a, \pm 2\lambda/a, \pm 3\lambda/a, \dots$$

Also $\cos^2 \alpha = 1$, so at the interference maxima

$$I = 4I_0 \left(\frac{\sin \beta}{\beta} \right)^2$$

where $\beta = (kb/2) \sin \theta = (\pi b/\lambda) \sin \theta$. Then:

$$p = 1: \sin \theta = \lambda/a; \beta = \frac{\pi b}{\lambda} \frac{\lambda}{a} = \pi(b/a); \frac{I}{4I_0} = \left(\frac{\sin \beta}{\beta} \right)^2 = \left(\frac{\sin(\pi/4)}{\pi/4} \right)^2 = 0.8106$$

$$p = 2: \sin \theta = 2\lambda/a; \beta = \frac{\pi b}{\lambda} \frac{2\lambda}{a} = 2\pi(b/a); \frac{I}{4I_0} = \left(\frac{\sin \beta}{\beta} \right)^2 = \left(\frac{\sin(\pi/2)}{\pi/2} \right)^2 = 0.4053$$

$$p = 3: \sin \theta = 3\lambda/a; \beta = \frac{\pi b}{\lambda} \frac{3\lambda}{a} = 3\pi(b/a); \frac{I}{4I_0} = \left(\frac{\sin \beta}{\beta} \right)^2 = \left(\frac{\sin(3\pi/4)}{3\pi/4} \right)^2 = 0.0901$$

- 11-20.** The irradiance is given by,

$$I = I_0 \left(\frac{\sin \beta}{\beta} \right)^2 \left(\frac{\sin N\alpha}{\alpha} \right)^2$$

with $N = 10$, $a = 5b$, $b = 10^{-4} \text{ cm}$, $\lambda = 435.8 \text{ nm}$. Recall that $\beta = \frac{\pi}{\lambda} b \sin \theta$, so $\alpha = 4\beta$. For interference maxima,

$$\left(\frac{\sin N\alpha}{\alpha} \right)^2 = 1 \Rightarrow I = I_0 \left(\frac{\sin \beta}{\beta} \right)^2$$

Also, $\sin \theta = m\lambda/a$ and $\beta = \frac{\pi b}{\lambda} \left(\frac{m\lambda}{a} \right) = m\pi(b/a) = m\pi/5$. Then,

$$\text{For } m = 1: I/I_0 = \left(\frac{\sin \beta}{\beta} \right)^2 = \left(\frac{\sin(\pi/5)}{\pi/5} \right)^2 = 0.875$$

$$\text{For } m = 2: I/I_0 = \left(\frac{\sin(2\pi/5)}{2\pi/5} \right)^2 = 0.573. \quad \text{For } m = 3: I/I_0 = \left(\frac{\sin(3\pi/5)}{3\pi/5} \right)^2 = 0.255$$

$$\text{For } m = 4: I/I_0 = \left(\frac{\sin(4\pi/5)}{4\pi/5} \right)^2 = 0.0547. \quad \text{For } m = 5: I/I_0 = \left(\frac{\sin(5\pi/5)}{5\pi/5} \right)^2 = 0.$$

- 12-4.** $\mathfrak{R} = mN = \frac{\lambda a v}{\Delta \lambda} = \frac{589.2935}{0.597} = 987$; $N = \frac{a}{m}$. So, for $m = 1$, $N = 987$ and for $m = 2$, $N = 494$.

- 12-6.** See Figure 12-14 that accompanies the statement of this problem in the text.

$$\mathfrak{R}(m = 3) = mN = (3)(16,000 \times 2.5) = 120,000$$

$$\mathfrak{R}(m = 2) = mN = (2)(16,000 \times 2.5) = 80,000$$

$$\Delta \lambda = \lambda/\mathfrak{R} = 550 \text{ nm}/80,000 = 0.006875 \text{ nm} = 0.069 \text{ \AA}$$

- 23-19.** Given $n_I = 5.3$ at $\lambda = 589.3 \text{ nm}$. (a) $\alpha = 4\pi n_I/\lambda = 4\pi(5.3)/(589.3 \text{ nm}) = 0.113 \text{ nm}^{-1}$

(b) $I = I_0 e^{-\alpha s}$. For $I = 0.01 I_0$, $e^{-\alpha s} = 0.01 \Rightarrow s = (-1/\alpha) \ln(0.01) = 40.75 \text{ nm} = 0.069 \lambda$

23-21. (a) The penetration depth is

$$|z|_{1/e} = \frac{1}{\alpha} = \frac{\lambda}{2\pi} \frac{1}{\sqrt{\sin^2 \theta / n^2 - 1}} = \frac{0.546 \mu\text{m}}{2\pi} \frac{1}{\sqrt{\sin^2(45^\circ) / (1/1.6)^2 - 1}} = 0.164 \mu\text{m}$$

(b) Since irradiance is proportional to the square of the field amplitude and with $\alpha = \frac{1}{|z|_{1/e}} = 6.089 \mu\text{m}^{-1}$,

$$\frac{I}{I_0} = e^{-2\alpha|z|} = e^{-2(6.089 \mu\text{m}^{-1})(1 \mu\text{m})} = 5.1 \times 10^{-6}$$

25-1. (a) Consider,

$$K \equiv n^2 = (n_R + i n_I)^2 = n_R^2 - n_I^2 + 2i n_I n_R = K_R + i K_I$$

$$K_R = n_R^2 - n_I^2, K_I = 2 n_I n_R$$

Solving these two relations for n_R and n_I proceeds as,

$$K_I = 2 n_I n_R = 2 n_I \sqrt{K_R^2 + n_I^2}$$

$$K_I^2 = 4 n_I^2 (K_R^2 + n_I^2)$$

$$4 n_I^4 + 4 K_R^2 n_I^2 - K_I^2 = 0$$

$$n_I^2 = \frac{-4 K_R \pm \sqrt{16 K_R^2 + 16 K_I^2}}{8} = \frac{-K_R \pm \sqrt{K_R^2 + K_I^2}}{2}$$

To make $n_I^2 > 0$, choose the + sign. Thus,

$$n_I = \left[\frac{-K_R + \sqrt{K_R^2 + K_I^2}}{2} \right]^{1/2}$$

$$n_R^2 = K_R + n_I^2 = \frac{2 K_R}{2} + \frac{-K_R + \sqrt{K_R^2 + K_I^2}}{2} = \frac{K_R + \sqrt{K_R^2 + K_I^2}}{2}$$

$$n_R = \left[\frac{K_R + \sqrt{K_R^2 + K_I^2}}{2} \right]^{1/2}$$

(b) If $K_I \approx K_R$,

$$n_R = \left[\frac{K_I + \sqrt{2 K_I^2}}{2} \right]^{1/2} = \sqrt{K_I} \left(\frac{1 + \sqrt{2}}{2} \right)^{1/2} = 1.099 \sqrt{K_I}$$

$$n_I = \left[\frac{-K_I + \sqrt{2 K_I^2}}{2} \right]^{1/2} = \sqrt{K_I} \left(\frac{-1 + \sqrt{2}}{2} \right)^{1/2} = 0.455 \sqrt{K_I}$$

25-7. (a) $\delta_{A1} = \left(\frac{2}{\sigma \mu_0 \omega} \right)^{1/2} = \left(\frac{2}{3.54 \times 10^7 (4\pi \times 10^{-7}) 2\pi \times 6 \times 10^4} \right)^{1/2} \text{ m} = 0.345 \text{ mm}$

(b) $\delta_{s.w.} = \left(\frac{3.54 \times 10^7}{4.3} \right) \times \delta_{A1} = 0.991 \text{ m} \approx 1 \text{ m}$

$$\mathbf{25-8.} \quad \delta_{Ag} = \left(\frac{\lambda}{\sigma \mu_0 \pi c} \right)^{1/2} = \left(\frac{0.1}{3 \times 10^7 (4 \pi \times 10^{-7}) \pi (3 \times 10^8)} \right)^{1/2} \text{ m} = 1.68 \times 10^{-6} \text{ m} = 1.68 \mu\text{m}$$

As long as the silver coating is thicker than this the silver-plated brass component would work.

$$\mathbf{25-9.} \quad (\text{a}) \quad I = I_0 e^{-\alpha x} \Rightarrow (I/I_0) = (1/4) = e^{-\alpha x} = e^{-\alpha(3.42\text{m})} \Rightarrow 3.42 \alpha = \ln(4) \Rightarrow \alpha = 0.405 \text{ m}^{-1}$$

$$(\text{b}) \quad (I/I_0) = (1/100) = e^{-(0.405 \text{ m}^{-1})x} \Rightarrow (0.405 \text{ m}^{-1})x = \ln(100) \Rightarrow x = 11.37 \text{ m}$$